























Maths Progression Statements























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1. Background:

These progression statements have been developed across the Trust through dialogue between Heads, Maths Leads and Teaching Staff. We have used the following as key source materials:

- National Curriculum Maths Programmes of Study 2014
- NCETM Progression Maps (with Reasoning)
- Third Space Learning The Ultimate Maths Vocabulary List 2018
- **NCETM Calculation Guidance 2015**
- White Rose National Curriculum Progression Y1-6 2019
- Power Maths Strand Yearly Overview 2019
- NCETM Maths Vocabulary List for Teachers KS1-3 2015
- NCETM Spine Overview Pilot Materials Y1-6 2018
- Early Years Progression Charts NCETM 2019
- Understanding Early Years Mathematics: The Connective Model Haylock and Cockburn (1989)
- Concrete, Pictorial and Abstract Approaches Jerome Bruner 1960 & Cockcroft Report 1982
- How People Learn: Brain, Mind, Experience and School (Bransford et al 2000), published by the National Academy of Sciences and the National Research Council

2. Purpose:

The progression statements are intended to be used to provide a robust framework upon which to build the Maths curriculum. They provide an assurance of:

- i. Sequential progressive learning of skills and knowledge within Maths. They support the step by step visiting and revisiting of strands within Maths to deepen understanding over time.
- ii. Mathematical conceptual approaches. Maths has a distinctive pedagogical approach through the development of the connective model, enabling children's understanding through the use of specific language, concrete manipulatives, mathematical symbols/representations and contexts. Therefore the approach that has been taken is to develop key areas or big ideas within Maths (substantive concepts) and group key vocabulary around them which are often themselves secondary concepts. These are attached in a separate document — Mathematical Concepts, Ideas and Vocabulary.
- iii. A secure framework from which schools and teachers can plan and create a sequential and connected curriculum mediated to the needs of their children and their context. There are particular links to Computing, Geography, Design Technology, Science and Art.
- iv. A basis for assessment and moderation within and between schools.

Learning is not always a linear progression. These statements are therefore a tool for teachers to adapt to the different needs of their cohorts, classes and individual children.





















3. Maths Concepts:

a) The Big Conceptual Picture

Mathematics is a creative and highly inter-connected discipline that has been developed over centuries, providing the solution to some of history's most intriguing problems. It is essential to everyday life, critical to science, technology and engineering, and necessary for financial literacy and most forms of employment. A high-quality mathematics education therefore provides a foundation for understanding the world, the ability to reason mathematically, an appreciation of the beauty and power of mathematics, and a sense of enjoyment and curiosity about the subject.

.Our disadvantaged children can face particular challenges due to their circumstances and therefore it is particularly important that they have opportunities to be learn mathematical vocabulary and be empowered through practical application and representations to discover and formulate their own thinking.

One of the strongest research summaries supporting the importance of conceptual understanding can be found in How People Learn: Brain, Mind, Experience and School (Bransford et al 2000), published by the National Academy of Sciences and the National Research Council:

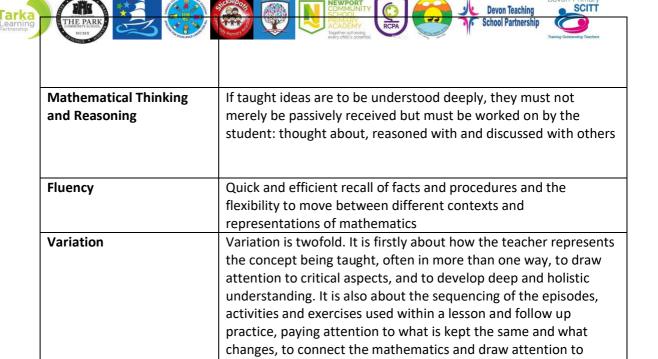
Experts' knowledge is **connected and organized around important concepts** (eg, mathematical fluency). To develop competence in an area of maths, students must: a) have a deep foundation of factual knowledge & recall, b) understand facts and ideas in the **context of a conceptual framework**, and c) organize knowledge in ways that facilitate retrieval and application organizing information into a conceptual framework allows for greater transfer; that is, it allows the student to apply what was learned in new situations and to learn related information more quickly

Anderson and Krathwohl's book (2001) updated Benjamin Bloom's Taxonomy of Educational Objectives (1956), and further supports the need to teach for deeper conceptual understanding. By separating factual knowledge from conceptual knowledge, we highlight the need for educators to teach for deep understanding of conceptual knowledge, not just for remembering isolated and small bits of factual knowledge (p 42). Students understand when they build connections between the "new" knowledge to be gained and their prior knowledge. More specifically, the incoming knowledge is integrated with existing schemas and cognitive frameworks. Since concepts are the building blocks for these schemas and frameworks, conceptual knowledge provides a basis for understanding

B) Five Big Ideas

Five main 'big ideas' recur within the Primary Maths teaching and which are useful for teachers to keep revisiting explicitly as they enable deeper understanding to develop in their modelling:

Teacher 'Big Ideas'	
Coherence	Lessons are broken down into small, connected steps that gradually unfold the concept, providing access for all children and leading to a generalisation of the concept and the ability to apply the concept to a range of contexts
Structure and Representation (See Connective Model & CPA Models below)	Representations used in lessons expose the mathematical structure being taught, the aim being that students can do the maths without recourse to the representation



mathematical relationships and structure.















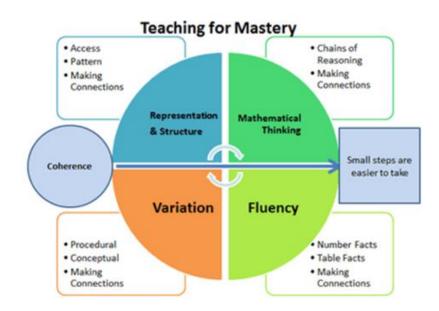








4. Pedagogical Approaches



i. Connective Model

Understanding mathematics involves identifying and understanding connections between mathematical ideas. Haylock and Cockburn (1989) suggested that effective learning in mathematics takes place when the learner makes cognitive connections. Teaching and learning of mathematics, especially when modelling, should therefore focus on making such connections. The connective model helps to make explicit the connections between different mathematical representations: symbols, mathematically structured images, language and contexts.

The interconnections represented by the lines in this image from Haylock and Cockburn is developed more fully through 'Talk for Learning' between pupils to extend their thinking.













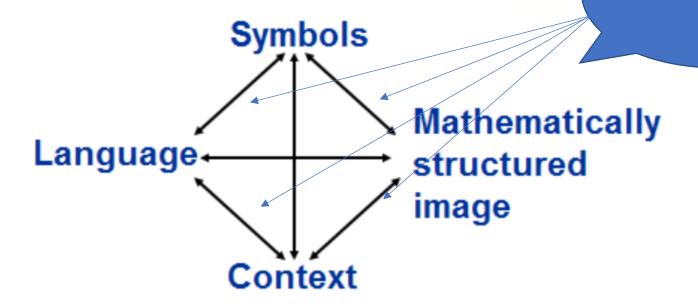








Talk for Learning



ii. Concrete, Pictorial, Abstract (CPA)

Children (and adults!) can find maths difficult because it is abstract. The Concrete Pictorial Abstract (CPA) approach is a system of learning that uses physical and visual aids to build a child's understanding of abstract topics.

Pupils are introduced to a new mathematical concept through the use of concrete resources (e.g. fruit, Dienes blocks etc). When they are comfortable solving problems with physical aids, they are given problems with pictures – usually pictorial representations of the concrete objects they were using.

Then they are asked to solve problems where they only have the abstract i.e. numbers or other symbols. Building these steps across a lesson can help pupils better understand the relationship between numbers and the real world, and therefore helps secure their understanding of the mathematical concept they are learning.

Eg:





















Calculation policy: Subtraction

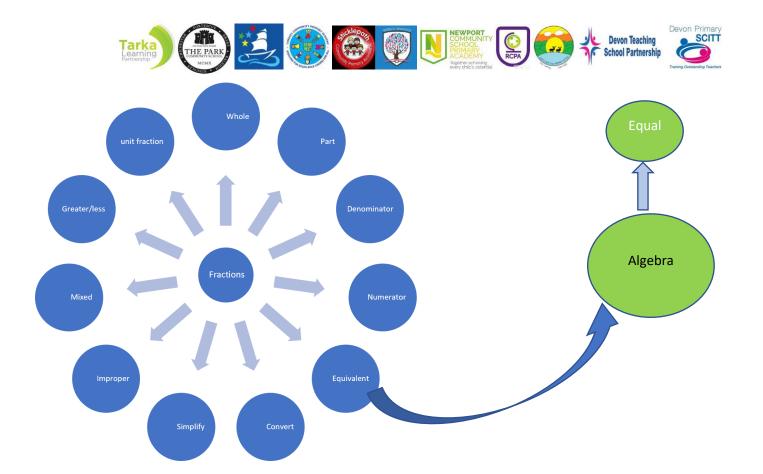
Key language: take away, less than, the difference, subtract, minus, fewer, decrease.

Concrete	Pictorial	Abstract
Physically taking away and removing objects from a whole (ten frames, Numicon, cubes and other items such as beanbags could be used).	Children to draw the concrete resources they are using and cross out the correct amount. The bar model can also be used.	4-3=
4 - 3 = 1	Ø Ø Ø Ø O	4 3 ?

5. Conceptual Development

Mathematical strands have primary conceptual areas. They also often having many secondary concepts/vocabulary attached to them (for example fractions will have equivalency, simplification, conversion etc). For this reason, Mathematical Concepts, Ideas and Vocabulary Maps have been produced (see end of document) which show the key understanding that is being developed across the overarching concept. As this schema is built up children can then begin linking different conceptual areas eg angles can be used within shapes, develop translations and coordinates.

Examples of Concepts, Ideas and Vocabulary Maps and how they might connect to build schemas















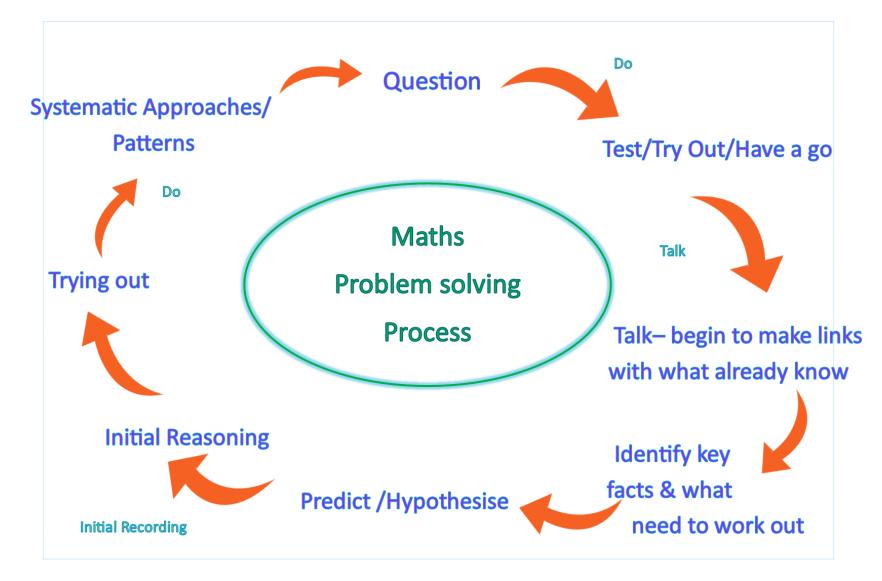




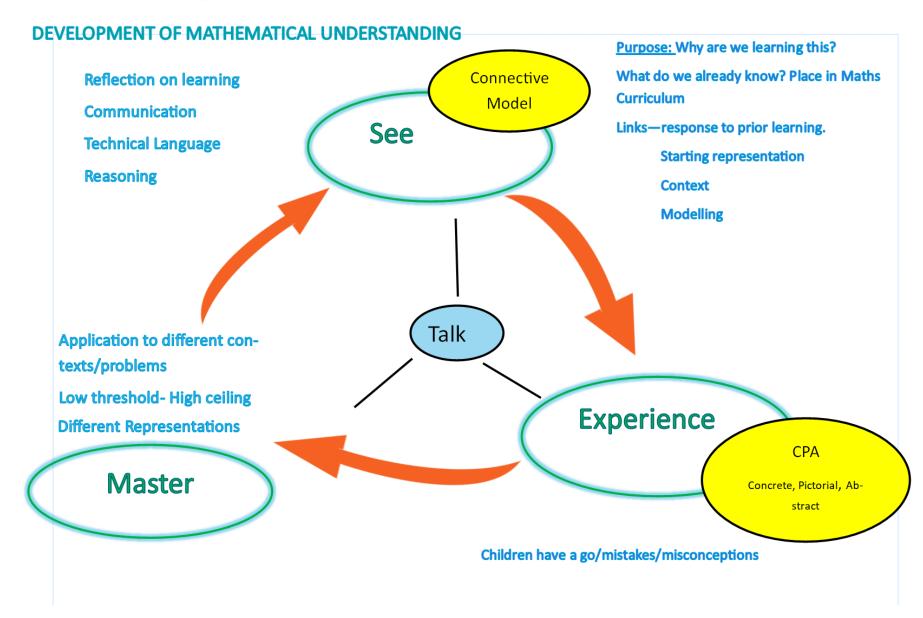




6. Mathematical SKILLS development-Working Mathematically -







7. Overarching Mathematical Skills





















Skill	Definition
Number sense	To have an understanding of a number through counting initially and then to see the relationships between numbers as they add, subtract, multiply and divide
Spatial sense -	The ideas of shape, size, space, position, direction, angle, dimension and movement.
"geometry."	
Representation	Making mathematical ideas "real" by using words, pictures, symbols, and objects
Measurement	Finding the length, height, capacity and weight of an object or distance using units like metres, litres, grams. Measurement is also of time (in minutes, days, years)
Estimation	This is the ability to make an approximation about the amount or size of something based of what a child might already know.
Patterns	Patterns, whether numbers, shapes or images, repeat in a logical way. Patterns help children learn to make predictions, to understand what comes next, to make logical connections, and to use reasoning skills.
Problem-solving	The ability to think through a problem, to recognize there is more than one path to the answer. It means using past knowledge, to look at alternatives and use logical thinking skills to find an answer.
Comparison	To recognise similarities and differences between numbers, shapes, scales(etc) and processes
Communicate	To explain, with reasoning, an idea or mathematical process clearly using examples / representations.
Self-question	To internalise a checking process as they move through a mathematical process – does this work? what might this do? Why is this so far from my estimate?





















8. Knowledge Progression

Primary Progression – Place Value



	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Place Value: Counting	count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number Count numbers to 100 in numerals; count in multiples of twos, fives and tens Autumn 1 Autumn 4 Spring 2 Summer 4	count in steps of 2, 3, and 5 from 0, and in tens from any number, forward and backward Autumn 1	count from 0 in multiples of 4, 8, 50 and 100; find 10 or 100 more or less than a given number Autumn 1 Autumn 3	count in multiples of 6, 7, 9, 25 and 1000 count backwards through zero to include negative numbers Autumn 1 Autumn 4	count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000 count forwards and backwards with positive and negative whole numbers, including through zero	
Place Value: Represent	identify and represent numbers using objects and pictorial representations read and write numbers to 100 in numerals read and write numbers from 1 to 20 in numerals and words. Autumn 1	read and write numbers to at least 100 in numerals and in words identify, represent and estimate numbers using different representations, including the number line Autumn 1	identify, represent and estimate numbers using different representations read and write numbers up to 1000 in numerals and in words Autumn 1	identify, represent and estimate numbers using different representations read Roman numerals to 100 (I to C) and know that over time, the numeral system changed to include the concept of zero and place value Autumn 1	read, write, (order and compare) numbers to at least 1 000 000 and determine the value of each digit read Roman numerals to 1000 (M) and recognise years written in Roman numerals. Autumn 1	read, write, (order and compare) numbers up to 10 000 000 and determine the value of each digit Autumn 1
	Autumn 4 Spring 2 Summer 4					





















Primary Progression - Place Value



	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Place Value : PV and Compare	given a number, identify one more and one less	 recognise the place value of each digit in a two-digit number (tens, ones) compare and order numbers from 0 up to 100; use <, > and = signs 	recognise the place value of each digit in a three-digit number (hundreds, tens, ones) compare and order numbers up to 1000	find 1000 more or less than a given number recognise the place value of each digit in a four-digit number (thousands, hundreds, tens, and ones) order and compare numbers beyond 1000	(read, write) order and compare numbers to at least 1 000 000 and determine the value of each digit	(read, write), order and compare numbers up to 10 000 000 and determine the value of each digit
Use	Autumn 1 Autumn 4 Spring 2 Summer 4	Autumn 1	Autumn 1	Autumn 1	Autumn 1	Autumn 1
Place Value: Problems& Rounding		use place value and number facts to solve problems.	solve number problems and practical problems involving these ideas	round any number to the nearest 10, 100 or 1000 solve number and practical problems that involve all of the above and with increasingly large positive numbers	interpret negative numbers in context round any number up to 1 000 000 to the nearest 10, 100, 1000, 10 000 and 100 000 solve number problems and practical problems that involve all of the above	round any whole number to a required degree of accuracy use negative numbers in context, and calculate intervals across zero solve number and practical problems that involve all of the above
4		Autumn 1	Autumn 1	Autumn 1	Autumn 1	Autumn 1





















Primary Progression - Addition & Subtraction



	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Addition & Subtraction: Recall, Represent, Use	read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs represent and use number bonds and related subtraction facts within 20	recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100 show that addition of two numbers can be done in any order (commutative) and subtraction of one number from another cannot recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems	estimate the answer to a calculation and use inverse operations to check answers	estimate and use inverse operations to check answers to a calculation	use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy	
	Autumn 2 Spring 1	Autumn 2	Autumn 2	Autumn 2	Autumn 2	





















Primary Progression - Addition & Subtraction



	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Addition & Subtraction: Calculations	add and subtract one- digit and two-digit numbers to 20, including zero	add and subtract numbers using concrete objects, pictorial representations, and mentally, including: a two-digit number and ones a two-digit number and tens two two-digit numbers adding three one-digit numbers	add and subtract numbers mentally, including; a three-digit number and ones a three-digit number and tens a three-digit number and hundreds add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction	add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate	add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction) add and subtract numbers mentally with increasingly large numbers	perform mental calculations, including with mixed operations and large numbers use their knowledge of the order of operations to carry out calculations involving the four operations
	Autumn 2 Spring 1	Autumn 2	Autumn 2	Autumn 2	Autumn 2	Autumn 2





















Primary Progression - Addition & Subtraction



	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Addition & Subtraction: Solve Problems	solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 = □ - 9	solve problems with addition and subtraction: using concrete objects and pictorial representations, including those involving numbers, quantities and measures applying their increasing knowledge of mental and written methods	solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction	solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why	solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign	solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why
	Autumn 2 Spring 1	Autumn 2	Autumn 2	Autumn 2	Autumn 2	Autumn 2





















Primary Progression - Multiplication & Division



	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Multiplication & Division: Recall, Represent, Use		recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot	recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables	recall multiplication and division facts for multiplication tables up to 12 × 12 use place value, known and derived facts to multiply and divide mentally, including: multiplying by 0 and 1; dividing by 1; multiplying together three numbers recognise and use factor pairs and commutativity in mental calculations	identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers know and use the vocabulary of prime numbers, prime factors and composite (non-prime) numbers establish whether a number up to 100 is prime and recall prime numbers up to 19 recognise and use square numbers and cube numbers, and the notation for squared (²) and cubed (³)	identify common factors, common multiples and prime numbers use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy.
		Autumn 4 Spring 1	Autumn 3	Autumn 4 Spring 1	Autumn 4	Autumn 2





















Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Multiplication & Division: Calculations	calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (x), division (+) and equals (=) signs Autumn 4	write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods Autumn 3	multiply two-digit and three-digit numbers by a one-digit number using formal written layout Series 1	multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers multiply and divide numbers mentally drawing upon known facts divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context multiply and divide whole numbers and those involving decimals by 10, 100 and 1000 Autumn 4 Autumn 4	multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context perform mental calculations, including with mixed operations and large numbers
	Spring 1	Spring 1	Spring 1	Spring 1 Summer 1	Autumn 2





















		ONIX .				
	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Multiplication & Division: Solve Problems	solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher	solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts	solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects	solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects	solve problems involving multiplication and division including using their knowledge of factors and multiples, squares and cubes solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates	solve problems involving addition, subtraction, multiplication and division
2	Summer 1	Autumn 4 Spring 1	Spring 1	Spring 1	Autumn 4 Spring 1	Autumn 2
Multiplication & Division: Combined Operations					solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign	use their knowledge of the order of operations to carry out calculations involving the four operations
ΣO					Spring 1	Autumn 2





















Primary Progression – Fractions, Decimals, Percentages



	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Fractions: Recognise and Write	recognise, find and name a half as one of two equal parts of an object, shape or quantity recognise, find and name a quarter as one of four equal parts of an object, shape or quantity	recognise, find, name and write fractions \frac{1}{3}, \frac{1}{4}, \frac{2}{4} \text{ and } \frac{3}{4} \text{ of a length, shape, set of objects or quantity} Spring 4	count up and down in tenths; recognise that tenths arise from dividing an object into 10 equal parts and in dividing one-digit numbers or quantities by 10 recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators recognise and use fractions as numbers: unit fractions and non-unit fractions with small denominators with small denominators with small denominators	count up and down in hundredths; recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten.	identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements > 1 as a mixed number [for example, \frac{2}{5} + \frac{4}{5} = \frac{6}{5} = 1\frac{1}{5}] Spring 2	
Fractions: Compare	Summer 2	Recognise the equivalence of ² / ₄ and ¹ / ₂	Spring 5 • recognise and show, using diagrams, equivalent fractions with small denominators • compare and order unit fractions, and fractions with the same denominators	Spring 3 • recognise and show, using diagrams, families of common equivalent fractions	compare and order fractions whose denominators are all multiples of the same number	use common factors to simplify fractions; use common multiples to express fractions in the same denomination compare and order fractions, including fractions > 1
		Spring 4	Summer 1	Spring 3	Spring 2	Autumn 3





















	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Fractions: Calculations		write simple fractions for example, \(\frac{1}{2}\) of 6 = 3	add and subtract fractions with the same denominator within one whole [for example, \frac{5}{7} + \frac{1}{7} = \frac{6}{7}]	add and subtract fractions with the same denominator	add and subtract fractions with the same denominator and denominators that are multiples of the same number multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams	 add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions multiply simple pairs of proper fractions, writing the answer in its simplest form [for example \frac{1}{4} \times \frac{1}{2} = \frac{1}{8}] divide proper fractions by whole numbers [for example, \frac{1}{3} + 2 = \frac{1}{6}]
		Spring 4	Summer 1	Spring 3	Spring 3	Autumn 3
Fractions: Solve Problems			solve problems that involve all of the above	solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number		
S			Spring 5 Summer 1	Spring 3		





















	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Decimals: Recognise and Write				recognise and write decimal equivalents of any number of tenths or hundredths recognise and write decimal equivalents to \(\frac{1}{4}, \frac{1}{2}, \frac{3}{4} \) Spring 4 Summer 1	read and write decimal numbers as fractions [for example, 0.71 = 71/100] recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents Spring 3	identify the value of each digit in numbers given to three decimal places Spring 1
Decimals: Compare				round decimals with one decimal place to the nearest whole number compare numbers with the same number of decimal places up to two decimal places Summer 1	round decimals with two decimal places to the nearest whole number and to one decimal place read, write, order and compare numbers with up to three decimal places Spring 3	

	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Decimals: Calculations & Problems				find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths find the effect of dividing the value of the digits in the answer as ones, tenths and hundredths	solve problems involving number up to three decimal places	multiply and divide numbers by 10, 100 and 1000 giving answers up to three decimal places multiply one-digit numbers with up to two decimal places by whole numbers use written division methods in cases where the answer has up to two decimal places solve problems which require answers to be rounded to specified degrees of accuracy
				Spring 4	Summer 1	Spring 1



















	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Fractions, Decimals and Percentages				solve simple measure and money problems involving fractions and decimals to two decimal places	recognise the per cent symbol (%) and understand that per cent relates to 'number of parts per hundred', and write percentages as a fraction with denominator 100, and as a decimal solve problems which require knowing percentage and decimal equivalents of \(\frac{1}{2}, \frac{1}{4}, \frac{1}{5}, \frac{2}{5}, \frac{4}{5} \) and those fractions with a denominator of a multiple of 10 or 25	associate a fraction with division and calculate decimal fraction equivalents [for example, 0.375] for a simple fraction [for example, \frac{3}{8}] recall and use equivalences between simple fractions, decimals and percentages, including in different contexts
Fracti				Spring 3 Spring 4 Summer 1	Spring 3	Spring 1 Spring 2





















	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Ratio and Proportion						solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts solve problems involving the calculation of percentages [for example, of measures, and such as 15% of 360] and the use of percentages for comparison solve problems involving similar shapes where the scale factor is known or can be found solve problems involving unequal sharing and grouping using knowledge of fractions and multiples. Spring 6























Primary Progression - Algebra



•	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
problem addit subtraction concurrence picto representations missing concurrence concurrenc	esentations, and ing number lems such as 7 =	recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems	solve problems, including missing number problems			use simple formulae generate and describe linear number sequences express missing number problems algebraically find pairs of numbers that satisfy an equation with two unknowns enumerate possibilities of combinations of two variables. Spring 3

Note - although algebraic notation is not introduced until Y6, algebraic thinking starts much earlier as exemplified by the 'missing number' objectives from Y1/2/3





















Primary Progression - Measurement



Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
• compare, describe and solve practical problems for: > lengths and heights [for example, long/short, longer/shorter, tall/short, double/half] > mass/weight [for example, heavy/light, heavier than, lighter than] > capacity and volume [for example, full/empty, more than, less than, half, half full, quarter] > time [for example, quicker, slower, earlier, later] • measure and begin to record the following: > lengths and heights > mass/weight > capacity and volume > time (hours, minutes, seconds)	 choose and use appropriate standard units to estimate and measure length/height in any direction (m/cm); mass (kg/g); temperature (°C); capacity (litres/ml) to the nearest appropriate unit, using rulers, scales, thermometers and measuring vessels compare and order lengths, mass, volume/capacity and record the results using >, < and = 	measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (I/mI)	Convert between different units of measure [for example, kilometre to metre; hour to minute] estimate, compare and calculate different measures	convert between different units of metric measure (for example, kilometre and metre; centimetre and millimetre; gram and kilogram; litre and millilitre) understand and use approximate equivalences between metric units and common imperial units such as inches, pounds and pints use all four operations to solve problems involving measure [for example, length, mass, volume, money] using decimal notation, including scaling	solve problems involving the calculation and conversion of units of measure, using decimal notation up to three decimal places where appropriate use, read, write and convert between standard units, converting measurements of length, mass, volume and time from a smaller unit of measure to a larger unit, and vice versa, using decimal notation to up to three decimal places convert between miles and kilometres
Spring 3 Spring 4 Summer 6	Spring 5 Summer 4	Spring 4 Summer 4	Autumn 3 Spring 2 Summer 3	Summer 1 Summer 4 Summer 5	Spring 4























Primary Progression - Measurement



	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Measurement: Money	recognise and know the value of different denominations of coins and notes	recognise and use symbols for pounds (£) and pence (p); combine amounts to make a particular value find different combinations of coins that equal the same amounts of money solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change	add and subtract amounts of money to give change, using both £ and p in practical contexts	estimate, compare and calculate different measures, including money in pounds and pence	use all four operations to solve problems involving measure [for example, money]	
	Summer 5	Autumn 3	Spring 2	Summer 2	Summer 1	























	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Measurement: Time	sequence events in chronological order using language [for example, before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening] recognise and use language relating to dates, including days of the week, weeks, months and years tell the time to the hour and half past the hour and draw the hands on a clock face to show these times	compare and sequence intervals of time tell and write the time to five minutes, including quarter past/to the hour and draw the hands on a clock face to show these times know the number of minutes in an hour and the number of hours in a day	tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24-hour clocks estimate and read time with increasing accuracy to the nearest minute; record and compare time in terms of seconds, minutes and hours; use vocabulary such as o'clock, a.m./p.m., morning, afternoon, noon and midnight know the number of seconds in a minute and the number of days in each month, year and leap year compare durations of events [for example to calculate the time taken by particular events or tasks]	read, write and convert time between analogue and digital 12- and 24-hour clocks solve problems involving converting from hours to minutes; minutes to seconds; years to months; weeks to days	solve problems involving converting between units of time	use, read, write and convert between standard units, converting measurements of time from a smaller unit of measure to a larger unit, and vice versa
	Summer 6	Summer 3	Summer 2	Summer 3	Summer 4	Year 5 Summer 4





















Primary Progression - Measurement



	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Measurement: Perimeter, Area, Volume			measure the perimeter of simple 2-D shapes	measure and calculate the perimeter of a rectilinear figure (including squares) in centimetres and metres find the area of rectilinear shapes by counting squares	measure and calculate the perimeter of composite rectilinear shapes in centimetres and metres calculate and compare the area of rectangles (including squares), and including using standard units, square centimetres (cm²) and square metres (m²) and estimate the area of irregular shapes estimate volume [for example, using 1 cm³ blocks to build cuboids (including cubes)] and capacity [for example, using water]	recognise that shapes with the same areas can have different perimeters and vice versa recognise when it is possible to use formulae for area and volume of shapes calculate the area of parallelograms and triangles calculate, estimate and compare volume of cubes and cuboids using standard units, including cubic centimetres (cm³) and cubic metres (m³), and extending to other units [for example, mm³ and km³]
			Spring 4	Autumn 3 Spring 2	Autumn 5 Summer 5	Spring 5





















Primary Progression - Geometry



	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Geometry: 2-D Shapes	recognise and name common 2-D shapes [for example, rectangles (including squares), circles and triangles]	identify and describe the properties of 2-D shapes, including the number of sides and line symmetry in a vertical line identify 2-D shapes on the surface of 3-D shapes, [for example, a circle on a cylinder and a triangle on a pyramid] compare and sort common 2-D shapes and everyday objects	draw 2-D shapes	compare and classify geometric shapes, including quadrilaterals and triangles, based on their properties and sizes identify lines of symmetry in 2-D shapes presented in different orientations	distinguish between regular and irregular polygons based on reasoning about equal sides and angles. use the properties of rectangles to deduce related facts and find missing lengths and angles	draw 2-D shapes using given dimensions and angles compare and classify geometric shapes based on their properties and sizes illustrate and name parts of circles, including radius, diameter and circumference and know that the diameter is twice the radius
	Autumn 3	Spring 3	Summer 3	Summer 5	Summer 2	Summer 1
Geometry: 3-D Shapes	recognise and name common 3-D shapes [for example, cuboids (including cubes), pyramids and spheres]	recognise and name common 3-D shapes [for example, cuboids (including cubes), pyramids and spheres]. compare and sort common 3-D shapes and everyday objects	make 3-D shapes using modelling materials; recognise 3-D shapes in different orientations and describe them		identify 3-D shapes, including cubes and other cuboids, from 2-D representations	recognise, describe and build simple 3-D shapes, including making nets
	Autumn 3	Spring 3	Summer 3		Summer 2	Summer 1





















Primary Progression - Geometry



	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Geometry: Angles & Lines			recognise angles as a property of shape or a description of a turn dentify right angles, recognise that two right angles make a half-turn, three make three quarters of a turn and four a complete turn; identify whether angles are greater than or less than a right angle identify horizontal and vertical lines and pairs of perpendicular and parallel lines	identify acute and obtuse angles and compare and order angles up to two right angles by size identify lines of symmetry in 2-D shapes presented in different orientations complete a simple symmetric figure with respect to a specific line of symmetry	know angles are measured in degrees: estimate and compare acute, obtuse and reflex angles draw given angles, and measure them in degrees identify: angles at a point and one whole turn (total 360°) angles at a point on a straight line and ½ a turn (total 180°) other multiples of 90°	find unknown angles in any triangles, quadrilaterals, and regular polygons recognise angles where they meet at a point, are on a straight line, or are vertically opposite, and find missing angles
			Summer 3	Summer 5	Summer 2	Summer 1























Primary Progression - Geometry



Year	1 Year 2	Year 3	Year 4	Year 5	Year 6
Geometry: Position & Direction & movement, whole, half, and three-turns	d combinations of including mathematical objects quarter in patterns and		describe positions on a 2-D grid as coordinates in the first quadrant describe movements between positions as translations of a given unit to the left/right and up/down plot specified points and draw sides to complete a given polygon	identify, describe and represent the position of a shape following a reflection or translation, using the appropriate language, and know that the shape has not changed	describe positions on the full coordinate grid (all four quadrants) draw and translate simple shapes on the coordinate plane, and reflect them in the axes
Summe	r 3 Spring 3 Summer 1		Summer 6	Summer 3	Autumn 4





















Primary Progression - Statistics



	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Statistics: Present and Interpret		interpret and construct simple pictograms, tally charts, block diagrams and simple tables Spring 2	interpret and present data using bar charts, pictograms and tables Spring 3	interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs Summer 4	complete, read and interpret information in tables, including timetables Autumn 3	interpret and construct pie charts and line graphs and use these to solve problems Summer 3
Statistics: Solve Problems		ask and answer simple questions by counting the number of objects in each category and sorting the categories by quantity ask and answer questions about totalling and comparing categorical data Spring 2	solve one-step and two-step questions [for example, 'How many more?' and 'How many fewer?'] using information presented in scaled bar charts and pictograms and tables Spring 3	solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs Summer 4	solve comparison, sum and difference problems using information presented in a line graph Autumn 3	calculate and interpret the mean as an average Summer 3



















EYFS	YEAR 1	YEAR 2	YEAR 3	YEAR 4	YEAR 5	YEAR 6
One more One less Place Order Number Count Numbers up to twenty Number line Pictorial Answer Equals Read Write	Same as EYFS, plus: Forwards Backwards Numerals Words Multiples Equal to More than Less than Fewer Most Least Identify Represe nt Digit Calculat e Odd Even Pattern Numbers up to one hundred	Same as EYFS & Year 1, plus: One s Ten s Two- digit Estimate Place Value Solve Problems Greater than > Less than < Nearest ten Number facts Partition Count in steps Zero Compare Determine Value	Same as EYFS & KS1, plus: Hundred s Three- digit ten more one hundred more ten less one hundred less Roman numeral Numbers up to one thousand	Same as previous year groups, plus: Thousands Four- digit Negative number One thousand more One thousand less Decimal Decimal place Rounding Place holder Nearest ten Nearest thousand One place Whole number Integer Tenths Hundredt	Same as previous year groups, plus: Ten thousands Hundred thousands Millions Context Steps of powers Decimal equivalents Two decimal places Thousandths Numbers up to one million	Same as previous year groups, plus Intervals across zero Three decimal places Hundredths Thousandths Ten thousandths Numbers up to ten million





















ADDITION AND SUBTRACTION VOCABULARY							
EYFS	YEAR 1	YEAR 2	YEAR 3	YEAR 4	YEAR 5	YEAR 6	
	Same as EYFS,	Same as EYFS &	Same as EYFS &	Same as previous	Same as previous	Same as previous	
	plus:	Year	KS1,				
A 1.1	One step problem	1, plus:	plus:	year groups, plus:	year groups, plus:	year groups, plus:	
Add	Concrete object	Columnar addition	Three-digit number	Two step problems	Increasingly large	Estimation	
Subtract	Pictorial	Columnar Subtraction	Hundreds	Context	numbers	Mixed operations	
Addition	representation	Tens	Estimate	Four-digit	More than 4 digits		
Subtraction	Missing number	Order	Number facts		Rounding		
Adding	Problem	Inverse			Determine		
Subtracting	Read	Relationship			Context		
Number	Write	Calculation			Multi-step		
					problems		
Number line	Interpret	Solve problems					
Single digit	Equals =	Missing number					
Count on	Signs	problems					
Count back	One-digit	Quantities					
Answer	Two-digit	Measures					
Doubling	Ones	Formal Written					
Halving	Mental	method					
Sharing	Mentally	Mental method					
Numbers to		Method					
twenty							
Check		Operation					
		Apply					
		Whole number					























EYF S	YEAR 1	YEAR 2	YEAR 3	YEAR 4	YEAR 5	YEAR 6
<u> </u>		Same as EYFS & Year	Same as EYFS & KS1,	Same as previous	Same as previous	Same as previous
		1, plus:	plus:	year groups, plus:	year groups, plus:	year groups, plus
	Multiples	Multiplication facts	Missing number	Derived facts	Decimals	Scale factor
	Twos	Division facts	problem	Factors	Four-digit	Long division
	Fives	Multiplication tables	Estimate	Factor pairs	Long multiplication	Whole number
	Tens	Odd numbers	Inverse	Scaling problems	Short division	remainders
	Number	Even numbers	Formal written	Three-digit	Remainders	Fractions
	Multiply	Share	method		Context	Rounding
	Divide	Equally	Mathematical		Common factors	Mixed operations
	Multiplication	Repeated division	statement		Common multiples	-
	Division	Calculate	Recall		Prime numbers	
	One step problem		Integer		Prime factors	
	Answer		Two- digit		Composite numbers	
	Concrete object		One- digit		Square number	
	Pictorial				Cube number	
	representation				Notation	
	Arrays				Squares	
	Count				Cubes	
	Equals					
	Write					



















			NS (INCLUDING NTAGES) VOCA			
EYF S	YEAR 1	YEAR 2	YEAR 3	YEAR 4	YEAR 5	YEAR 6
	Fraction Half Equal parts One whole Object Shape Quantity Quarter	Same as EYFS & Year 1, plus: Simple fractions Equivalent equivalence Count	Same as EYFS & KS1, plus: Tenths Unit fractions Non- unit fractions Numerator Denominator Compare Order Add Subtract Solve problems	Same as previous year groups, plus: Hundredths Decimal Decimal place One decimal place Two decimal places Round decimals Whole number Common equivalent fractions Decimal equivalents Dividing Ones Tenths Hundredths Simple measure Money problems	Same as previous year groups, plus: Thousandt hs Multiples Three decimal places Per cent Number of parts per hundred Percentages Decimal fraction Mixed numbers Improper fraction Proper fraction Convert Mathematic al statements Multiply Percentage and decimal	Same as previous year groups, plus: Common factors Common multiple Decimal fraction equivalents Simplest form





















			JREMENT VOCA			
EY FS	YEAR 1	YEAR 2	YEAR 3	YEAR 4	YEAR 5	YEAR 6
	Same as EYFS,	Same as EYFS &	Same as EYFS &	Same as	Same as	Same as
Measure	plus: Length	Year 1, plus:	KS1, plus:	previous year	previous year	previous year
Measurem	Height	Greater than	Duration	groups, plus:	groups, plus:	groups, plus:
ent Size	Long	> Less than	Time	Estimate	Square	Decimal
Weight	Short	< Equals =	taken	Rectilinear	centimetres	notation Cubic
Capaci	Longer	Intervals	Nearest	figure Area	(cm2)	centimetres
ty	Shorter	Standard	minute	Rectilinear	Square metres	(cm3)
Compa	Tall	units	Record	shapes Convert	(m2) Irregular	Cubic metres
re .	Double	Estimate	Seconds		shapes Volume	(m3) Cubic
Solve	Half	Direction	a.m.		(cm3) Cubes	millimetre
Proble	Mass	Temperature	p.m.		Cuboids	(mm3)
ms	Heavy	Unit	noon		Square	Cubic
Object	Light	Scale	midnigh		numbers	kilometre
Time	Heavier than	s	l t		Cube	(Km3)
	Lighter than	Ruler	kilometr		numbers	Decimal
	Volume	s	e add		Metric	places
	Full	Thermometers	subtract		measure	formulae
	Empty	Measuring	millimetre		Metric units	Miles
	More than	vessels Metres	s		Imperial units	
	Less than	Centimetres	perimeter		Inches	
	Half	Kilograms	simple 2-D		Pound	
	Half full	Grams	shapes		s	
	Quarter	Degrees	analogue clock		Pints	
	Quicker	Celsius Litres	roman			
	Slower	Millilitres	numerals 12-			
	Earlier	Symbols	hour			
	Later	Money	24-hour			
	Sequence events	Pounds (£)	Leap			
	Chronological	Pence (p)	year			
	order	Different				
	Before	combinatio				
		ns Change				
		Five past				





















After	Ten past		
Next	Quarter past		
First	Twenty past		
Toda	Twenty-five		
у	past Half past		
Yesterda	Twenty-five to		
у	Twenty to		
Tomorro	Quarter to		
w	Ten to		
Morning	Five to		
Afternoo			
n			
Evening			
Record			
Hours			
Minutes			
Hour			
Half past			
O clock			
Hands			
Clock			
face			
Seconds			
Coins			
Notes			
Dates			
Days			
Weeks			
Months			
Years			





















EYF	YEAR 1	YEAR 2	YEAR 3	YEAR 4	YEAR 5	YEAR 6
S						
	Same as EYFS,	Same as EYFS &	Same as EYFS &	Same as	Same as	Same as
Shape	plus: 2-D Shapes	Year 1, plus:	KS1, plus:	previous year	previous year	previous year
Square	3-D Shapes	Propertie	Angl	groups, plus:	groups, plus:	groups, plus:
Rectangl	Two-	s	е	Lines of	Angles	Radius
e Circle	Dimensional	Compare	Turn	symmetry	Measure	Diameter
Triangle Sides	Three-	Common	Right angles	Symmetric	Degrees	Circumference
Straight side	Dimensional	Line	Quarter of a	figure Classify	Missing	Nets
Curved side	Cuboid	symmetry	turn Half-turn	Geometric	lengths	
	Cube	Vertical line	Three quarters	shapes	Missing	
	Pyrami	Edges	of a turn	Quadrilaterals	angles	
	d Cone	Faces	Complete turn	Acute angle	Regular	
	Cylind	Vertices	Horizontal lines	Obtuse angle	polygons	
	er	Pentago	Vertical lines		Irregular	
	Sphere	n	Perpendicular		polygons	
		Hexago	lines Parallel		Degrees	
		n	lines		Estimate	
		Heptago			compare	
		n			Reflex angle	
		Octagon			Point	
		Nonago			Straight	
		n			line	
		Decagon			Multiples	



















Kite			
Rhom	b		
us			
Polyg	on		
Squa	e-based		
pyran	nid Triangular		
pyran	nid Triangular		
prism	Rectangular		
	Pentagonal		
	Hexagonal		
	Octagonal		
	Octahedron		
Dode	cahedron		
Tetra	nedron		
Recta	ngular		
pyran	_		
	gonal		
	nid Hexagonal		
	nid Octagonal		
pyran			





















	GEO	METRY: POSIT	TON AND DIREC	CTION VOCABL	JLARY	
EYF S	YEAR 1	YEAR 2	YEAR 3	YEAR 4	YEAR 5	YEAR 6
	Same as EYFS, plus:	Same as EYFS & Year	Same as EYFS & KS1,	Same as previous	Same as previous	Same as previous
Position	Half turn	1, plus:	plus:	year groups, plus:		year groups, plus:
Distance Direction	Quarter turn	Rotation		Co-ordinates	Reflection	Four quadrants
Move	Three-quarter turn	Right angle		Quadrant		
Movement	Left	Clockwise		Grid		
Patterns	Right	Anti-clockwise		Translate		
	Up	Order		Translation		
	Down	Arrange		Axis		
		Sequence		X- axis		
				Y-axis		
				Spaces		
				Unit		
				Plot		
				Point		
				Polygon		





















		STA	TISTICS VOCABI	ULARY		
EYF S	YEAR 1	YEAR 2	YEAR 3	YEAR 4	YEAR 5	YEAR 6
		Interpret	Same as KS1, plus:	Same as previous	Same as previous	Same as previous
		Construct	Present	year groups, plus:	year groups, plus:	year groups, plus:
		Pictogram	Presented	Time graphs	Timetables	Pie chart Calculate
		Tally chart	Graph	Comparison	Line graph	Mean
		Block diagrams	Statistics	Problems		Average
		Horizontal	Bar charts			
		Vertical	Tables			
		x- axis	Solve			
		y-axis	One- step			
			questions			
		key	Two- step			
		title	questions Information			
		chart title	information			
		Simple tables Ask				
		Ask				
		Questions				
		Counting				
		Objects				
		Category				
		Sort				
		Quantity				
		Total				
		Compare				
		Data				





















		ALG	SEBRA VOCABL	JLARY		
EYF S	YEAR 1	YEAR 2	YEAR 3	YEAR 4	YEAR 5	YEAR 6
	Same as EYFS, plus: Solve One-step problem Missing number Check Calculate problem Sequence Chronological	Same as EYFS & Year 1, plus: Inverse Relationship Compare Order Arrange Pattern	Same as EYFS & KS1, plus:	Same as previous year groups, plus: Perimeter Algebra Algebraically	Same as previous year groups, plus: Properties Rectangles Deduce Related facts Missing lengths Missing angles	Same as previous year groups, plus: Missing number Problem Pairs Number sentence Variables Combination Possibility Enumerate Equation Formulae Generate Linear number sequence





















9. MATHEMATICAL CONCEPTS, IDEAS AND VOCABULARY – examples of useful concept maps











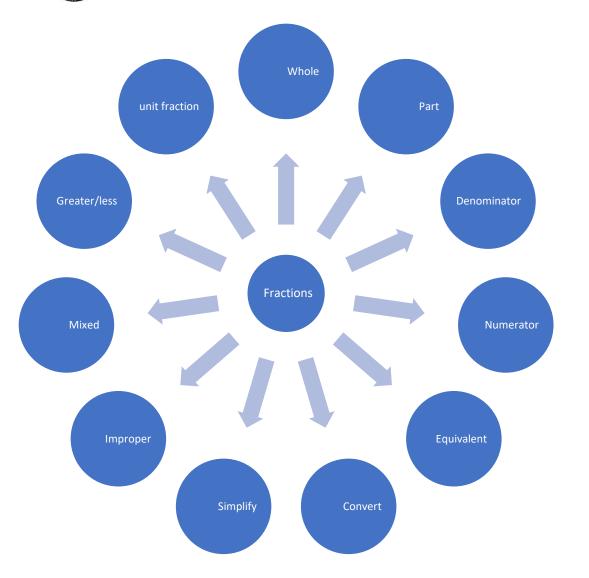






















































Use the template below to take the key concept and attached vocabulary for the year group to create your own 'concept map' for the area of Maths you are teaching:

